

# Reserve Accumulation, Macroeconomic Stabilization and Sovereign Risk

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Javier Bianchi<sup>1</sup>      César Sosa-Padilla<sup>2</sup>

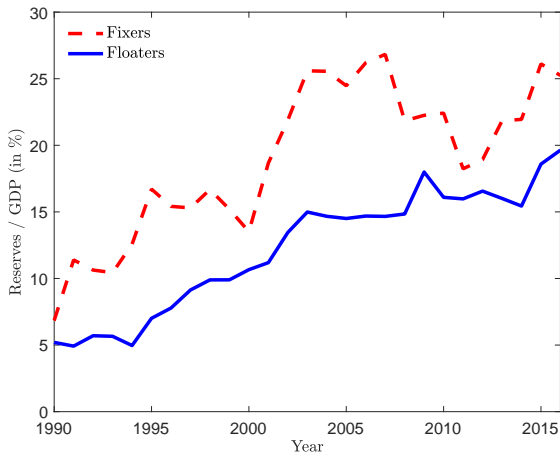
2018 SED Annual Meeting

<sup>1</sup>Minneapolis Fed & NBER

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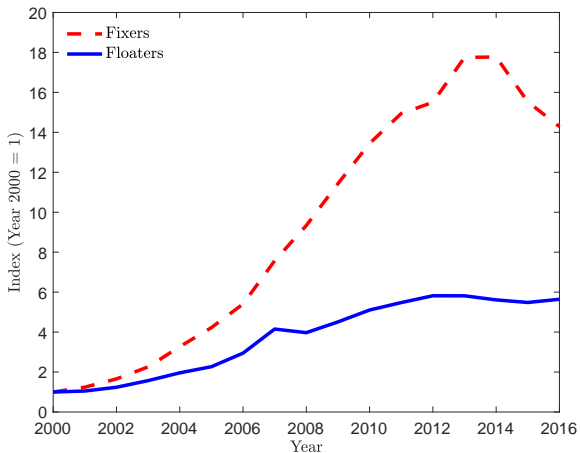
# Motivation

EMEs with fixed exchange rates hold more foreign reserves ...



# Motivation (ctd)

... and have accumulated reserves faster.



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- Share of countries w/ less flexible exchange rates 60% – 80% (Ilzetzki et. al. 2017)
- Has gone up w/ adoption of Euro among Adv. Economies

## Motivation (ctd)

Conventional view: central banks w/ fixed exchange rate hold more reserves to prevent speculative attacks on currencies (Krugman)

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In this paper, we explore an alternative channel linking precautionary motives and macroeconomic stabilization

- Show that this is a quantitatively important channel to explain observed levels of reserves.

Sovereign default model with long-term debt and **foreign reserve accumulation**, and **downward wage rigidity**.

- Rollover risk induces large fluctuations in borrowing costs
- When borrowing costs are high, aggregate demand contracts causing involuntary unemployment
- Holdings of reserves (liquid assets) allow to mitigate fall in demand and increase in unemployment
- In good times, government issues debt and buy reserves for macroeconomic stabilization

# Main Elements of the Model

- Small open economy (SOE) with  $T - NT$  goods:
  - Stochastic endowment for tradables  $y^T$
  - Non-tradables produced with labor:  $y^N = F(h)$
- Wages are downward rigid in domestic currency
  - With fixed exchange rate,  $\pi^* = 0$  and L.O.P.,  $\Rightarrow$  wages are rigid in tradable goods  $w \geq \bar{w}$
- Government issues non-contingent long-duration bonds ( $b$ ) and saves in one-period risk free assets ( $a$ ), all in units of  $T$
- Default entails one-period exclusion and utility loss  $\phi(y)$
- Risk averse foreign lenders  $\rightarrow$  “risk-premium shocks”

# Households

- Households' preferences over consumption

$$\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \{u(c_t)\}$$

$$c = C(c^T, c^N) = [\omega(c^T)^{-\mu} + (1 - \omega)(c^N)^{-\mu}]^{-1/\mu}$$

- Budget constraint in units of tradables

$$c_t^T + p_t^N c_t^N = y_t^T + \phi_t^N + w_t h_t^s - \tau$$

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- Endowment of hours  $\bar{h}$ , but  $h_t^S < \bar{h}$  when  $w \geq \bar{w}$  binds.

- Optimality

$$p_t^N = \frac{1 - \omega}{\omega} \left( \frac{c_t^T}{c_t^N} \right)^{1+\mu}$$

- Maximize profits given by

$$\phi_t^N = \max_{h_t} p_t^N F(h_t) - w_t h_t$$

- $w_t$ : price of non-tradables and wages in units of tradables
- Firms' optimality condition is

$$p_t^N F'(h_t) = w_t$$

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# Asset/Debt Structure

- Long-term bond:
  - Bond pays  $\delta [1, (1 - \delta), (1 - \delta)^2, (1 - \delta)^3, \dots]$
  - Law of motion for bonds  $b_{t+1} = b_t(1 - \delta) + i_t$
  - price is  $q$

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- Government's budget constraint if **repay**:

$$g + q_a a_{t+1} + b_t \delta = \tau_t + a_t + \underbrace{q_t (b_{t+1} - (1 - \delta)b_t)}_{i_t \text{ debt issuance}}$$

- Government's budget constraint in **default**:

$$g + q_a a_{t+1} = \tau_t + a_t$$

## Foreign Investors

- Pricing kernel is a function of innovation to domestic output  $\varepsilon$  and a global factor  $\nu = \{0, 1\}$  (assumed to be independent)

$$m_{t,t+1} = e^{-r - \nu(\kappa\varepsilon_{t+1} + 0.5\kappa^2\sigma_\varepsilon^2)}, \quad \text{with } \kappa \geq 0,$$

- Implies constant risk free rate:

$$\mathbb{E}_{s'|s} m(s, s') = e^{-r} = q_a$$

- Bond price given by:

$$q = \mathbb{E}_{s'|s} \{ m(s, s')(1 - d') [\delta + (1 - \delta) q'] \}$$
$$d' = \hat{d}(a', b', s'), \quad q' = q(a'', b'', s')$$

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- Risk premium  $\geq 0$  if default occurs with low  $\varepsilon$  and  $\nu = 1$

## Recursive Problem

$$V(b, a, y^T) = \max_{d \in \{0,1\}} \left\{ (1-d)V^r(b, a, y^T) + dV^d(a, y^T) \right\}$$

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**Value of repayment:**

$$V^r(b, a, y^T) = \max_{b', a', h, c^T} \left\{ u(c^T, F(h)) + \beta \mathbb{E}_{y^{T'} | y^T} \left[ V(b', a', y^{T'}) \right] \right\}$$

subject to

$$c^T + g + q_a a' = a + y^T + q(b', a', y^T)(b' - (1-\delta)b) - \delta b \quad [\lambda]$$

$$\bar{w} \leq \frac{1-\omega}{\omega} \left( \frac{c^T}{F(h)} \right)^{1+\mu} F'(h) \quad [\xi]$$

$$h \leq \bar{h} \quad [\eta]$$

## Recursive Problem (ctd)

**Value of default:**

$$V^d(a, y^T) = \max_{c^T, h, a'} \left\{ u(c^T, F(h)) - \psi_d(y^T) + \beta \mathbb{E}_{y^{T'} | y^T} \left[ V(0, a', y^{T'}) \right] \right\}$$

subject to

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## Optimality Conditions – Labor Market

Assume  $F(h) = h^\alpha$  with  $\alpha \in (0, 1)$ .

Also assume **(just for simplicity)**:  $\mu = 0$ .

Optimality in labor market implies:

$$h^d(w) = \left( \frac{1 - \omega}{\omega} \right) \frac{\alpha}{w} c^T$$

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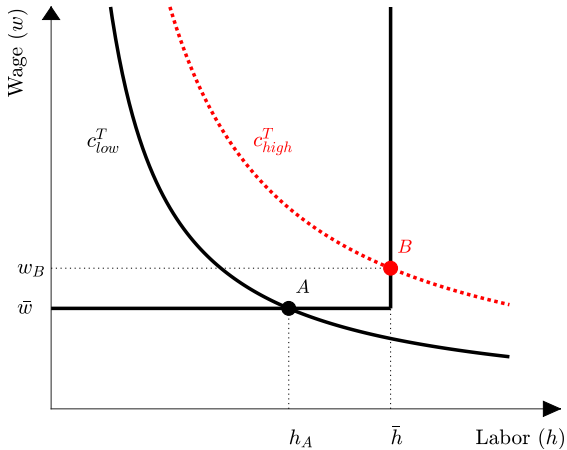
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# Labor Market Equilibrium



# Optimality Conditions

FOC wrt  $c^T$ :

$$c^T : \quad u_T + \xi \quad \left( \frac{1 - \omega}{\omega} \right) \frac{\alpha}{\bar{w}} = \lambda$$

$\xi \rightarrow$  multiplier on the  $w \geq \bar{w}$  constraint

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Tradable consumption has 2 benefits:

1. direct utility
2. reduction of unemployment

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Tradable consumption has 2 benefits:

1. direct utility
2. reduction of unemployment

For labor, we have:

$$h : u_N \alpha h^{\alpha-1} = \eta + \xi,$$

$\eta \rightarrow$  multiplier on the  $h \leq \bar{h}$  constraint



## Optimal Portfolio: gains from borrowing to buy reserves

Let  $\tilde{a}$  denote reserves that can be purchased when issuing an additional unit of debt for an initial state  $s$ :

$$\tilde{a} = \frac{q(\tilde{a}, b', s) + \frac{\partial q(\tilde{a}, b', s)}{\partial b'}}{q_a - \frac{\partial q(\tilde{a}, b', s)}{\partial a'}}.$$

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The future marginal benefit of doing this is:

$$\mathbb{E}_{s'|s} \left\{ \underbrace{\underbrace{\partial \tilde{a}}_{\text{Reserves}} (u'(c') + \xi' \Delta)}_{\text{Mg. utility benefits}} - \underbrace{[\delta + (1 - \delta)q'](1 - d')(u'(c') + \xi' \Delta)}_{\text{Debt repayments}} \right\}_{\text{Mg. utility costs}}$$

- Reserves pay-off in all states  $\rightarrow$  high marginal value when unemployment is high  $\Rightarrow$  macroeconomic stabilization

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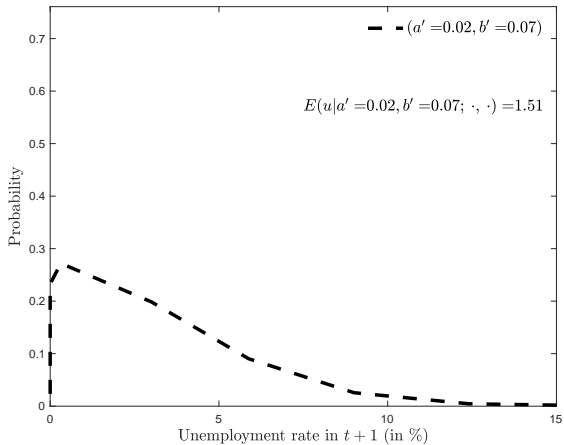
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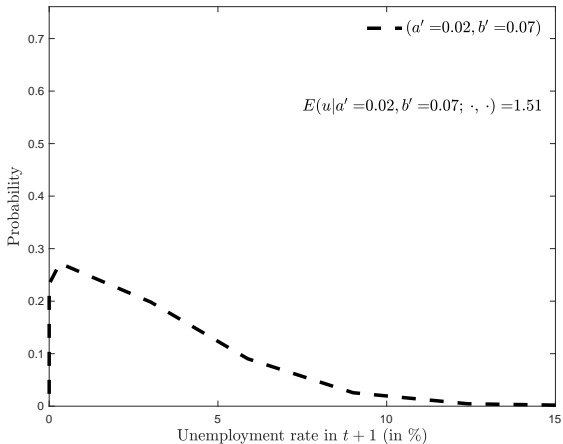
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- Reserves pay-off in all states  $\rightarrow$  high marginal value when unemployment is high  $\Rightarrow$  macroeconomic stabilization
- Debt repayments relatively less costly in bad times (when  $q'$  is low)

# Higher reserves can reduce future unemployment

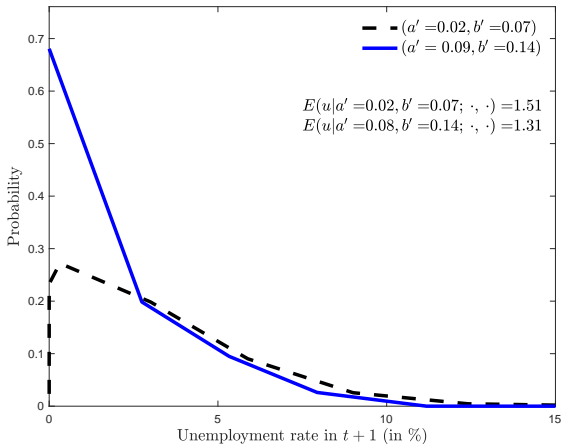


# Higher reserves can reduce future unemployment



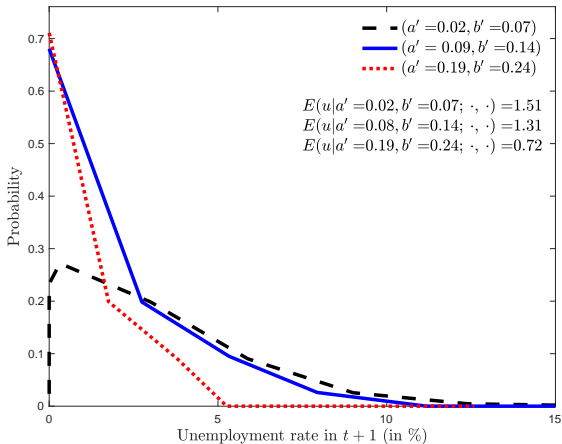
**Now:** consider a policy that **issues** debt to **increase** reserves, keeping NFA **constant**.

# Higher reserves can reduce future unemployment



**Note:** NFA is constant across portfolios → higher reserves can reduce future unemployment

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- Today: Calibrate flexible wage economy (Bianchi, Hatchondo and Martinez) and show effects of wage rigidity.
- 1 model period = 1 year.
- Use Mexican data (archetypical EME).



**Utility function:**

$$u(c) = \frac{c^{1-\gamma} - 1}{1-\gamma}, \text{ with } \gamma \neq 1$$

**Utility cost of defaulting:**

$$\psi_d(y^T) = \alpha_0 + \alpha_1 \log(y^T)$$

**Tradable income process:**

$$\log(y_t^T) = (1 - \rho)\mu_y + \rho \log(y_{t-1}^T) + \epsilon_t$$

with  $|\rho| < 1$  and  $\epsilon_t \sim N(0, \sigma_\epsilon^2)$

## Quantitative Analysis (ctd)

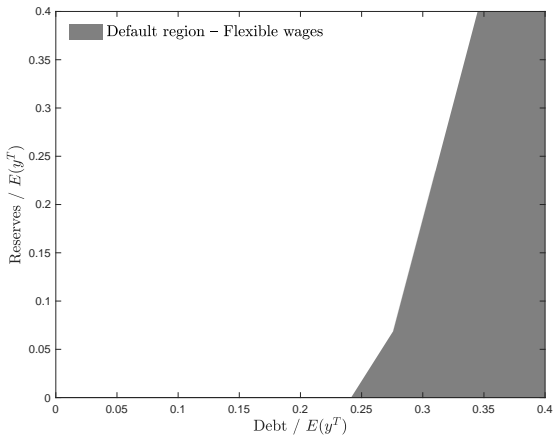
Parameter	Description	Value
$r$	Risk-free rate	0.04
$\beta$	Domestic discount factor	0.92
$\pi_{LH}$	Prob. of transiting to high risk-premium	0.15
$\pi_{HL}$	Prob. of transiting to low risk-premium	0.8
$\sigma_\epsilon$	Std. dev of innovation to $\log(y^T)$	0.034
$\rho$	Autocorrelation of $\log(y^T)$	0.66
$\mu_y$	Mean of $\log(y^T)$	$-\frac{1}{2}\sigma_\epsilon^2$
$g$	Government consumption	0.12
$\delta$	Coupon decaying rate	0.2845
$\omega$	Share of tradables	0.3
$1 + \mu$	Inverse of the intratemporal elast. of subs.	$\gamma$
Parameters set by simulation		
$\alpha_0$	Default cost parameter	2.45
$\alpha_0$	Default cost parameter	19
$\kappa_H$	Pricing kernel parameter	23
$\gamma$	Coefficient of relative risk aversion	3.3
$\bar{w}$	Lower bound on wages	1.25

1. Simulations moments.
2. Default sets and spreads.
3. Welfare exercises.

## Results: data and simulation moments

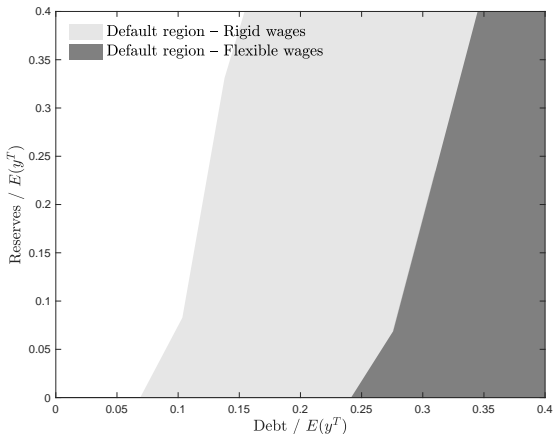
	Data	Model	
		Flex. $w$	Rigid $w$
<b>Targeted</b>			
$\sigma(c)/\sigma(y)$	1.0	1.0	1.0
Mean debt ( $b/y^T$ )	43.0	44.6	17.1
Mean $r_s$	2.4	2.5	2.4
$\Delta r_s$ w/ risk-prem. shock	2.0	2.0	1.6
<b>Non-Targeted</b>			
$\sigma(r_s)$	0.9	2.0	1.9
$\rho(r_s, y)$	-0.5	-0.8	-0.8
$\rho(c, y)$	0.8	0.9	0.9
Mean Reserves ( $a/y^T$ )	8.5	7.3	14.4
Mean Reserves/Debt ( $a/b$ )	0.20	0.17	0.85
Unemployment	3.9	0.0	2.8

## Results: default regions



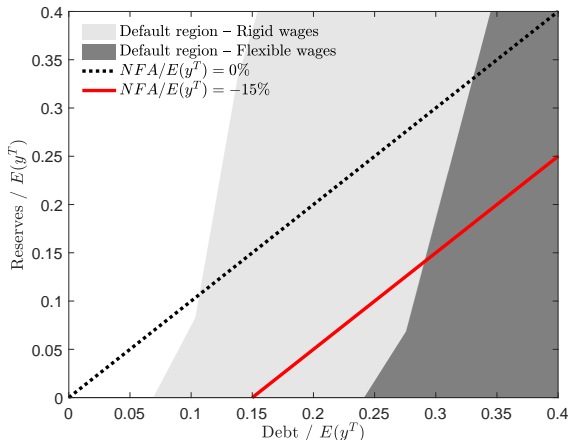
- Default incentives **increase** in debt and **decrease** in reserves.

## Results: default regions



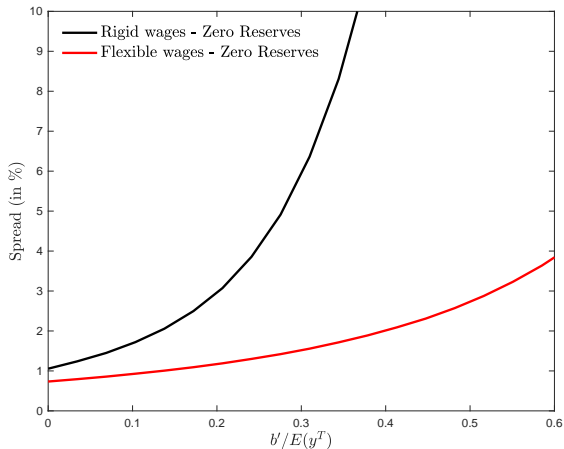
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- Wage rigidity **increases** default incentives

## Results: default regions and NFA



- Default incentives **increase** in debt and **decrease** in reserves.
- Wage rigidity **increases** default incentives
- Gross positions matter for default.

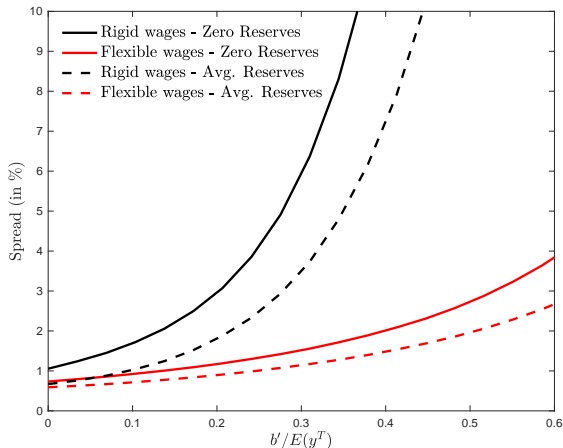
## Results: spreads, reserves and wage rigidity



- Wage rigidity increases spreads.



## Results: spreads, reserves and wage rigidity



- Wage rigidity **increases** spreads.
- Reserves **decrease** spreads, and **more** when wages are rigid. 29/35

## Results: welfare

We'll compute **welfare gains** of 'moving' from a **baseline** economy to an **alternative** economy:

$$\text{Welfare gain} = 100 \times \left[ \left( \frac{(1-\gamma)(1-\beta)V_{\text{alternative}} + 1}{(1-\gamma)(1-\beta)V_{\text{baseline}} + 1} \right)^{1/(1-\gamma)} - 1 \right]$$

We're interested in studying:

- Gains of eliminating wage rigidity
- Gains of being having access to reserves

To do the latter: define a “No-Reserves” economy (which can have or not wage rigidity).

## Results: welfare gains of eliminating wage rigidity

Baseline	Alternative	Welf. Gain
Benchmark w/ wage rigidity	Benchmark w/ flexible wage	2.48
No-Reserves w/ wage rigidity	No-Reserves w/ flexible wage	4.80

- Eliminating wage rigidity is **welfare enhancing**.
- Even **more** when **reserve accumulation is not possible**.

▶ plots

## Results: welfare gains of access to reserve accumulation

Baseline	Alternative	Welf. Gain
No-Reserves w/ flexible wage	Benchmark w/ flexible wage	0.15
No-Reserves w/ wage rigidity	Benchmark w/ wage rigidity	2.41

- Being able to accumulate reserves is **welfare enhancing**.
- Even **more** when facing **wage rigidities**.

▶ plots

# Conclusions

- Studied use of foreign reserves for macro stabilization goals in a SOE with:
  1. nominal rigidities
  2. fixed exchange rates, and
  3. sovereign default risk
- When borrowing costs are high, aggregate demand contracts causing involuntary unemployment
- Holdings of reserves (liquid assets) allow to mitigate fall in demand and increase in unemployment
- In good times, government issues debt and buy reserves for macroeconomic stabilization

## Conclusions (ctd)

We found that:

- Mechanism is **quantitatively relevant**:
  - Avg. reserves are twice as large.
  - Avg. reserves/debt ratio is 4 times as large.
- Wage rigidity increase default incentives and spreads.
- Reserves decrease default incentives and spreads.
- **Reserves** help **reduce** future **unemployment risk**.
- There are **sizeable welfare gains** of: accumulating reserves and eliminating wage rigidities.

## Conclusions (ctd)

Other implications:

- Maastricht clauses establish limits for gross debt positions in Eurozone
- Analysis suggests that minimum holdings of assets should be established.
  - A stock of foreign reserves might mitigate temptations to exit

**THANKS !**



We use the IMF Classif. of Exch. Rate Arrangements (as of 2016)

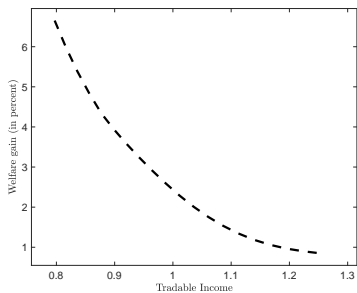
We follow Kondo and Hur (2016) and focus on 23 EMEs:

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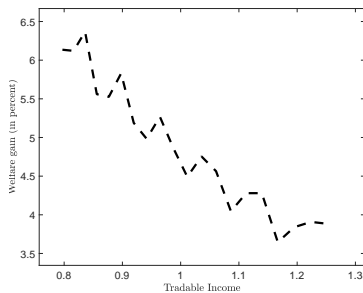
Argentina	India	Poland
Brazil	Indonesia	Romania
Chile	Malaysia	Russia
China	Mexico	South Africa
Colombia	Morocco	South Korea
Czech Republic	Pakistan	Thailand
Egypt	Peru	Turkey
Hungary	Philippines	

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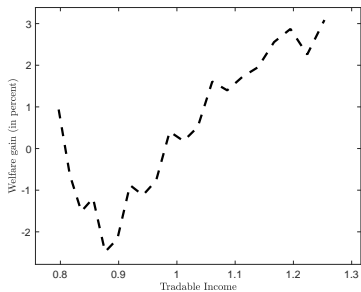
**Table 1:** EME classification: follow Financial Times and the London Stock Exchange (FTSE), Morgan Stanley Capital International (MSCI), the Economist, Standard & Poor's (S&P), and Dow Jones Indexes.



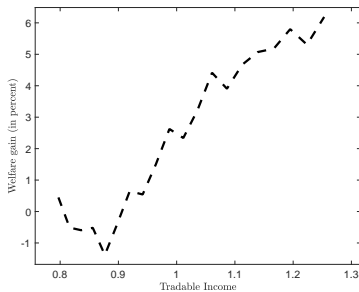
**Figure 1:** Benchmark



**Figure 2:** No-Reserves



**Figure 3:** Flexible wages



**Figure 4:** Rigid wages

## Results: welfare gains of eliminating wage rigidity

Initial debt = Avg. in simulations (14%). Initial reserves = zero.

<b>Baseline</b>	<b>Alternative</b>	<b>Welf. Gain</b>
Benchmark w/ wage rigidity	Benchmark w/ flexible wage	3.31
No-Reserves w/ wage rigidity	No-Reserves w/ flexible wage	4.81

- Eliminating wage rigidity is **welfare enhancing**.
- Even **more** when **reserve accumulation is not possible**.

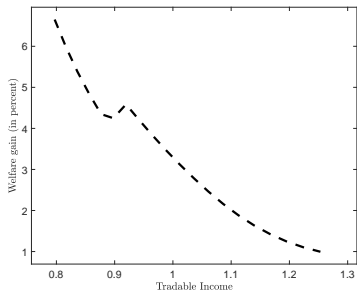
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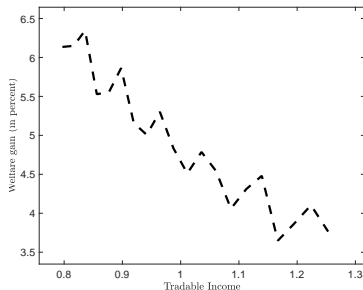
Baseline	Alternative	Welf. Gain
No-Reserves w/ flexible wage	Benchmark w/ flexible wage	-0.32
No-Reserves w/ wage rigidity	Benchmark w/ wage rigidity	1.12

- Being able to accumulate reserves can be **welfare enhancing**, especially with **wage rigidities**.

Initial debt = Avg. in simulations (14%). Initial reserves = zero.

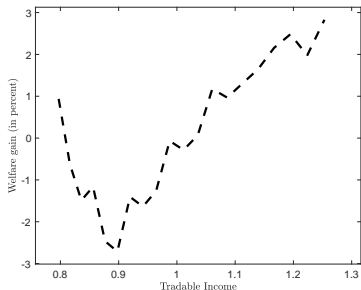


**Figure 5:** Benchmark

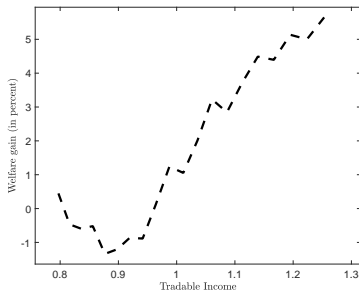


**Figure 6:** No-Reserves

Initial debt = Avg. in simulations (14%). Initial reserves = zero.



**Figure 7:** Flexible wages



**Figure 8:** Rigid wages